

School of Mathematical and Computational Sciences
Indian Association for the Cultivation of Science
Compiler Construction: COM 5202
Tutorial V (04 February 2026)

M. Sc Semester IV: 2025-2026

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Exercise 1.

[10]

Consider the following grammar.

$$\begin{aligned} P &\rightarrow \mathbf{prog} \ DLO \ \mathbf{start} \ CL \\ DLO &\rightarrow DLO \ DL \mid \varepsilon \\ DL &\rightarrow TY \ VL \\ TY &\rightarrow \mathbf{int} \mid \mathbf{real} \\ VL &\rightarrow VL \ \mathbf{id} \mid \mathbf{id} \\ CL &\rightarrow CL \ C \mid C \\ C &\rightarrow IC \mid OC \mid AC \\ IC &\rightarrow \mathbf{in} \ \mathbf{id} \\ OC &\rightarrow \mathbf{out} \ E \mid \mathbf{out} \ \mathbf{str} \\ AC &\rightarrow \mathbf{id} : E \\ E &\rightarrow E + T \mid E - T \mid T \\ T &\rightarrow T * F \mid T / F \mid F \\ F &\rightarrow \mathbf{ic} \mid \mathbf{rc} \mid \mathbf{id} \mid (E) \end{aligned}$$

The terminals are { **prog**, **start**, **int**, **real**, **in**, **out**, **ic**, **rc**, **id**, **str**, **:**, **+**, **-**, *****, **/**, **(**, **)** }.

The non-terminals are { *P*, *DLO*, *DL*, *TY*, *VL*, *CL*, *C*, *IC*, *OC*, *AC*, *E*, *T*, *F* }.

The start symbol is *P*.

The regular expressions are,

id: [A-Z] [_a-zA-Z0-9]*

ic: 0|[1-9][0-9]*

rc: [0-9]+\.[0-9]*((e|E)[+-]?[1-9][0-9]?)?

str: (\"[^"]*\")

Comment: (\/\/.*\n)

Write flex specification for the set of terminals of the grammar. The name of the flex file should be `lex.l`. The header file for it is `y.tab.h`. The header file defines some of the token values and the type of `yy1Type`.

We take the ASCII codes as token values for all single character terminals.

The scanner ignores a comment, but keeps track of the line number.

```
// y.tab.h
#ifndef _Y_TAB_H
#define _Y_TAB_H

#define ID      300
#define IC      301
#define RC      302
#define STR     303
#define PROG   304
#define START   305
```

```

#define REAL 306
#define INT 307
#define IN 308
#define OUT 309
#define NOTOK 400

```

```

int yylex(void);
typedef union {
    int integer ;
    double real;
char *string;
} yylType;

#endif

```

The scanner function `yylex()` will be called from `main()` in `myLex.c` (include `y.tab.h` in `myLex.c`). The `main()` function calls `yylex()` and prints the stream of tokens (shown in Input/Output). You may use the following Makefile for the process of compilation.

The input is from the `stdin`. You may write the input in a file and redirect it:

```
$ ./a.out < data
```

Makefile:

```

objfiles = myLex.o lex.yy.o

a.out: $(objfiles)
    cc $(objfiles)

myLex.o:      myLex.c y.tab.h
    cc -c -Wall myLex.c

lex.yy.o:    lex.yy.c
    cc -c lex.yy.c

lex.yy.c:    lex.l y.tab.h
    flex lex.l

clean:
    rm a.out lex.yy.c $(objfiles)

```

Finally prepare a `.tar` file using the following command.

```
$ tar cvf <roll no>.5.tar y.tab.h lex.l myLex.c Makefile
```

Send the `.tar` file to `goutamamartya@gmail.com`.

Input-Output

```

$ ./a.out
prog
<prog>
int

```

```

<int>
Factorial
<ID, Factorial>
factorial
Invalid characters: factorial
1234
<IC, 1234>
1234.567e-2
<RC, 12.345670>
"Indian Association for
the Cultivation of
Science"
<STR, Indian Association for
the Cultivation of
Science>
Value1: A1+B2*50/(X5-11)
<ID, Value1> <:> <ID, A1> <+> <ID, B2> <*> <IC, 50> </> <(> <ID, X5> <-> <IC, 11> <)>

```

Input from a data file.

```

// The file name is d0
prog
  int N
  real X1
start
  out "Give an integer"
  in N
  X1: N/13 - N*12
  out X1

```

Output

```

$ ./a.out < d0
<prog>
<int> <ID, N>
<real> <ID, X1>
<start>
<out> <STR, Give an integer>
<in> <ID, N>
<ID, X1> <:> <ID, N> </> <IC, 13> <-> <ID, N> <*> <IC, 12>
<out> <ID, X1>

```

Exercise 2. Consider the context-free grammar

$$S \rightarrow S S + \mid S S * \mid a$$

and the string $aa + a^*$

- (a) Give a leftmost derivation for the string.
- (b) Give a rightmost derivation for the string.
- (c) Give a parse tree for the string.

- (d) Is the grammar *ambiguous* or *unambiguous*?
- (e) Describe the language generated by the grammar.

Exercise 3.

- (a) Write the language of the grammar $S \rightarrow 0 S 1 \mid 0 1$ in set notation.
- (b) Remove left-recursion for the grammar $S \rightarrow S S + \mid S S * \mid a$ and then left-factor it.
- (c) Show that the grammar $S \rightarrow (S) \mid SS \mid \varepsilon$ is ambiguous. Is there any equivalent unambiguous grammar?

Exercise 4. We extend the CFG production rules as follows: regular expressions of grammar symbols are used in the right-hand side of production rules with proper meta symbols. Does this extension of notation extend the class of languages beyond CFL?

Exercise 5. Consider the following grammar G_5 with terminal symbols $\{+, *, (,), 0, 1\}$ and E as the start symbol.

$$\begin{aligned} E &\rightarrow E + T \mid T \\ T &\rightarrow T F \mid F \\ F &\rightarrow F * \mid P \\ P &\rightarrow (E) \mid 0 \mid 1 \end{aligned}$$

- (a) Informally define $L(G_5)$.
- (b) Remove left-recursion and form the grammar G_{5b} .
- (c) Find $First()$ and $Follow()$ of different non-terminals.
- (d) Draw the parse tree corresponding to $0 * +(01)^*$ following the *First* and *Follow* information.